

Recipes for Writing Algorithms for Atmospheric Corrections and  
Temperature/Emissivity Separations in the Thermal  
Regime for a Multi-Spectral Sensor

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# *Introduction*

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## **Atmospheric corrections:**

- In the visible uses dark targets (vegetation, water)
- In the thermal:
  - Global Data Assimilation System (GDAS) data for atmosphere (ASTER) If the atmospheric temperature and water vapor profile is known the measured radiances can be corrected for path radiance and attenuation
  - Atmospheric retrievals from sounding channels (e.g. MODIS and ASTER) Special sounding channels provide means of measuring the atmospheric temperature and water vapor profiles directly
  - “Robust water temperature retrievals” (e.g. ATSR, MTI). “Robust” means the retrieval minimizes the influence of the atmosphere.
  - “Physics based water temperature retrievals” (e.g. MTI) “Physics based” means that we solve physics based equations to retrieve atmospheric parameters as well as surface temperature.

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## *Physics based water temperature retrieval*

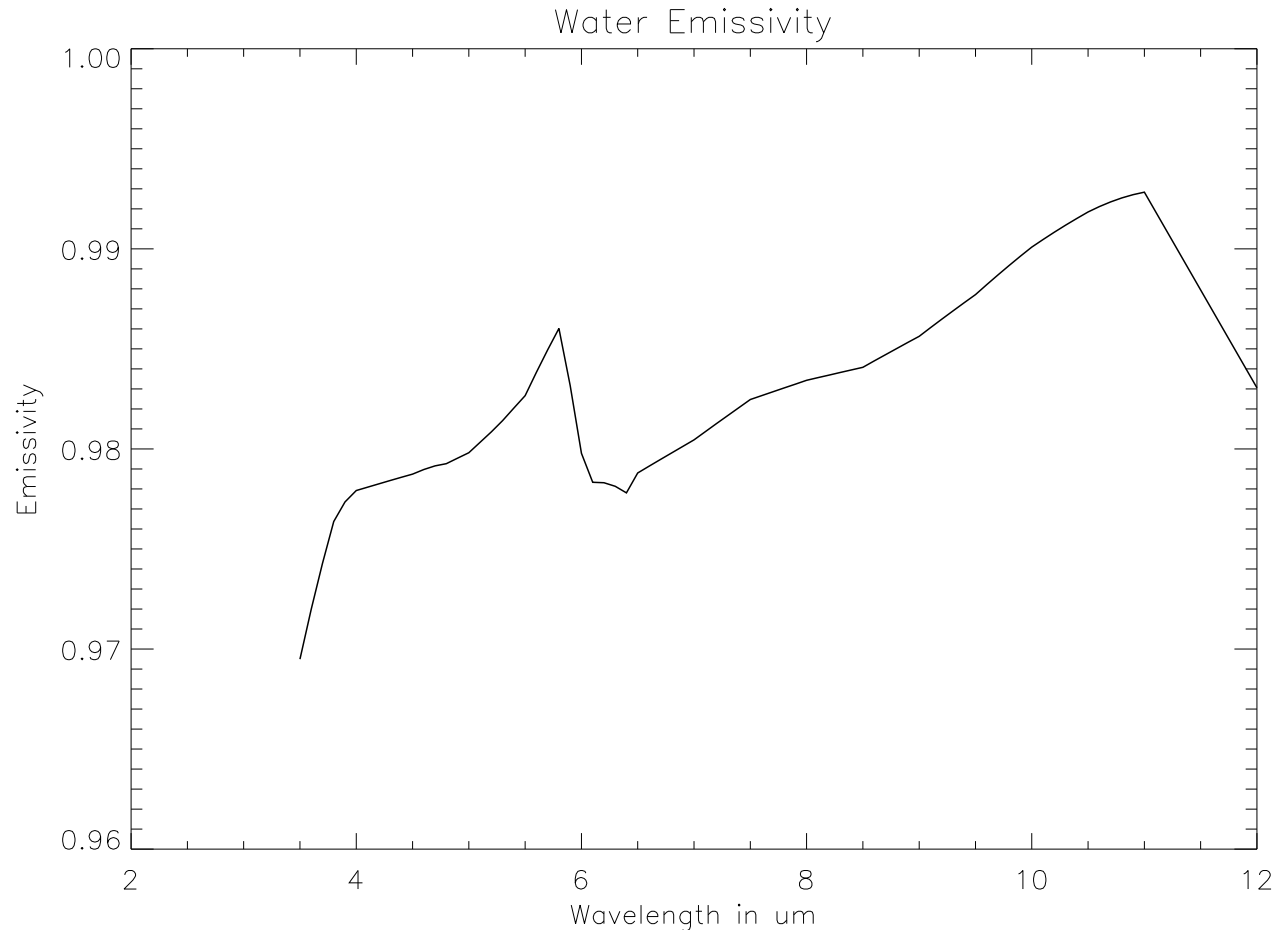
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### **Observations:**

1. The problem of temperature-emissivity separation which usually requires solving for  $(N + 1)$  unknowns can be simplified in the case of a known surface emissivity, such as water, to solving for the temperature only.
2. A correct solution of (1) through an atmospheric correction of the sensor radiance should lead to the **same skin temperature for all multi-spectral channels using the same atmospheric parameters.**

Note that in reality an additional atmospheric correction needs to be performed which requires knowledge of the atmospheric parameters such as columnar water vapor and atmospheric temperature.

## Water emissivity model for 10 deg view zenith, 4 m/s windspeed



Currently used models: *Cox-Munk*, Monte Carlo raytracing model based on *Pierson and Moskowitz (1964)*, *Preisendorfer and Mobley, (1986)* sea surface spectra

## A simple radiative transfer model for multi-spectral sensors (1):

Measured spectral radiance  $L_{m,\lambda}(H)$  along a ray reaching the sensor at height  $H$  and wavelength  $\lambda$  is:

$$\begin{aligned} L_{m,\lambda}(H) &= L_{\lambda}(\text{surface}) + L_{\lambda}(\text{path}) + L_{\lambda}(\text{reflected downwelling}) \quad (1) \\ &= \varepsilon_{w,\lambda} B_{\lambda}(T_w) \tau_{\lambda} + \int_0^H B_{\lambda}(T_a(z)) \kappa_{\lambda}(z) dz \\ &\quad + (1 - \varepsilon_{w,\lambda}) \tau_{\lambda} \int_H^0 B_{\lambda}(T_a(z)) \kappa_{\lambda}(z) dz, \end{aligned}$$

where  $\varepsilon_{w\lambda}$  is the water emissivity and  $B_{\lambda}(T)$  is the Planck function in units of  $W/(m^2 \mu m \text{ sr})$ .  $T_w$  is the skin temperature and  $T_a(z)$  is the atmospheric temperature profile. The atmospheric transmission is  $\tau_{\lambda}$  and  $\kappa_{\lambda}(z) = (\delta\tau_{\lambda}(z))/(\delta z)$ .

### Assumptions:

1. We neglect the reflected down-welling radiance of the atmosphere. The radiance is small in spectral bands with good atmospheric transmission and water surfaces reflect less than 3 %.
2. For simplicity we assume a one-layer model where  $\kappa_{\lambda}(z) = \kappa_{0,\lambda} \rightarrow \tau_{\lambda} = \kappa_{0,\lambda} H$  and  $T_a(z) = \text{const}$  which we'll call the effective atmospheric temperature. The path radiance can be approximated by:  $L_{\lambda}(\text{path}) = B_{\lambda}(T_a)[1 - \tau_{\lambda}(CW)]$ , where  $CW$  is the columnar water vapor amount. This approximation is quite good in atmospheric windows and its validity was tested using MODTRAN for MTI's spectral channels which lie in atmospheric window regions.

## A simple radiative transfer model for multi-spectral sensors (2):

Measured spectral radiance at wavelength  $\lambda$  is:

$$L_{m,\lambda} = \varepsilon_{w,\lambda} B_{\lambda}(T_w) \tau_{\lambda}(CW) + B_{\lambda}(T_a)[1 - \tau_{\lambda}(CW)]. \quad (2)$$

Solving eq(2) for the skin temperature  $T_w$  we find:

$$T_w = B_{\lambda}^{-1} \left[ \frac{L_{m,\lambda} - B_{\lambda}(T_a)[1 - \tau_{\lambda}(CW)]}{\varepsilon_{w,\lambda} \tau_{\lambda}(CW)} \right], \quad (3)$$

where the function  $B^{-1}$  is the inverse Planckian. For a multi-spectral instrument we need to integrate eq (3) over a range of wavelengths which results in:

$$T_w = B_i^{-1} \left[ \int_{\lambda(i)_a}^{\lambda(i)_b} \frac{L_{m,\lambda} - B_{\lambda}(T_a)[1 - \tau_{\lambda}(CW)]}{\varepsilon_{w,\lambda} \tau_{\lambda}(CW)} d\lambda \right], \quad (4)$$

where  $B_i^{-1}$  is an inverse Planckian for channel  $i$ .

Approximation of eq (4) is necessary to break the integral into two parts, one for the numerator and one for the denominator:

$$T_w \approx B_i^{-1} \left[ \frac{L_{m,i} - \int B_{\lambda}(T_a)[1 - \tau_{\lambda}(CW)] d\lambda}{\int \varepsilon_{w,\lambda} \tau_{\lambda}(CW) d\lambda} \right]. \quad (5)$$

Note: It is virtually impossible to eq (4) without an error for a multi-spectral sensor because we do not measure  $L_{m\lambda}$ !

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## *Look-up-table generation*

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1. Read the spectral emissivity data  $\varepsilon_\lambda$ ,
2. Read the spectral response data  $R_\lambda(i)$  for all thermal channels  $i$  and normalize the integral over  $R_\lambda$  to unity:

$$R_\lambda^* = \frac{R_\lambda}{\int_{\lambda(i)_a}^{\lambda(i)_b} R_\lambda d\lambda},$$

3. Read the MODTRAN derived spectral transmission  $\tau_\lambda$ ,
4. Interpolate the spectral emissivity to the same wavelength grid as the transmission,
5. Numerically integrate the products over each filter band  $i$  for a columnar water vapor amount  $CW$ :

(a) where the average transmission in band  $i$  is:

$$\tau_i(CW) = \int_{\lambda(i)_a}^{\lambda(i)_b} R_\lambda^* \tau_\lambda(CW) d\lambda,$$

(b) where the average of emissivity times transmission in band  $i$  is:

$$(\varepsilon\tau)_i(CW) = \int_{\lambda(i)_a}^{\lambda(i)_b} R_\lambda^* \varepsilon_\lambda \tau_\lambda(CW) d\lambda,$$

6. Store  $\tau_i(CW)$  and  $(\varepsilon\tau)_i(CW)$  in a table which can be read quickly.



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## *Finding the optimum water temperature*

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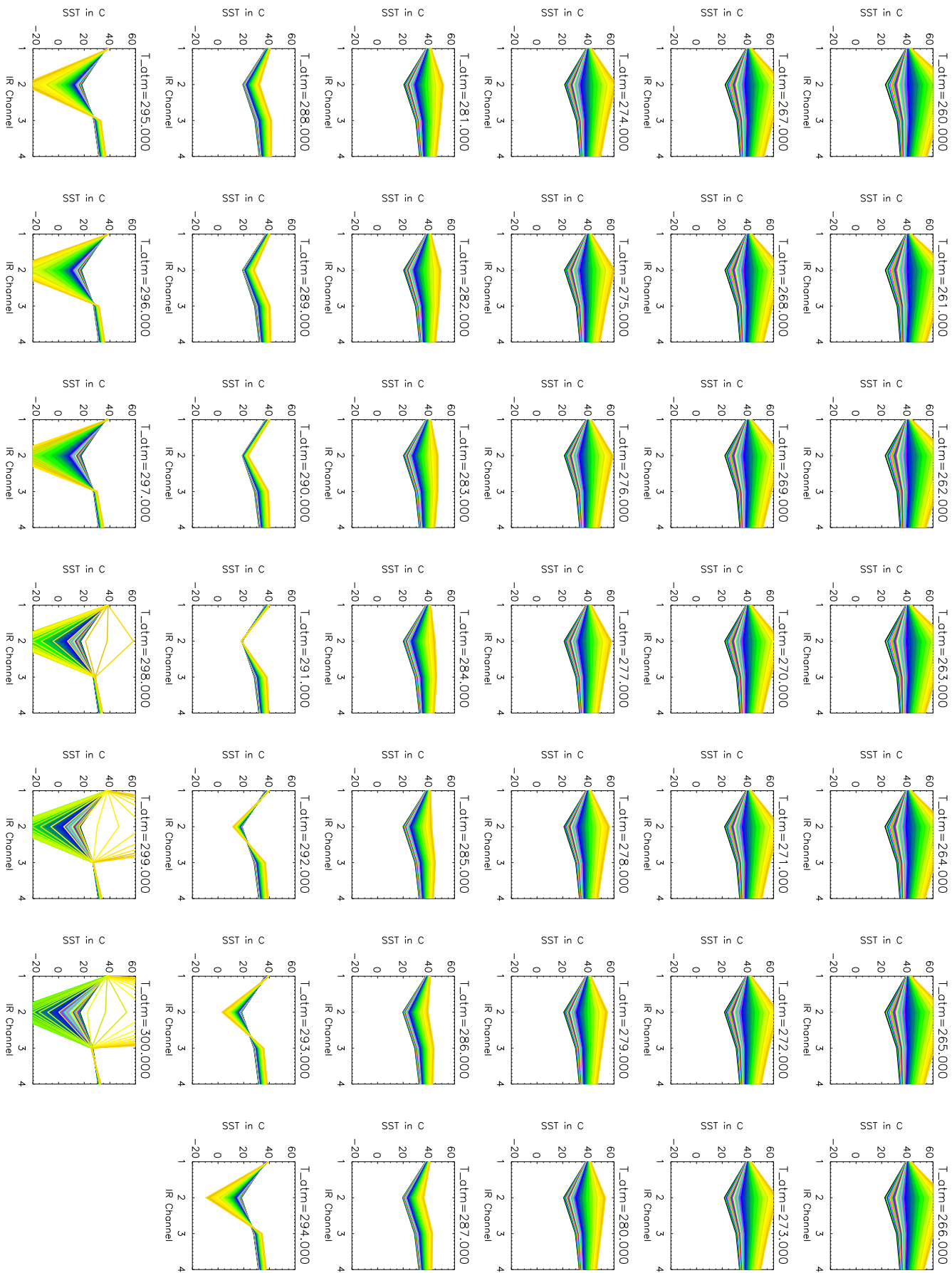
### Steps:

1. Find a pixel with water in the image.
2. For a selected atmosphere  $k$  (e.g. mid-latitude winter, US standard, ...):
  - (a) Compute the estimated water temperature in channel  $i$  using:

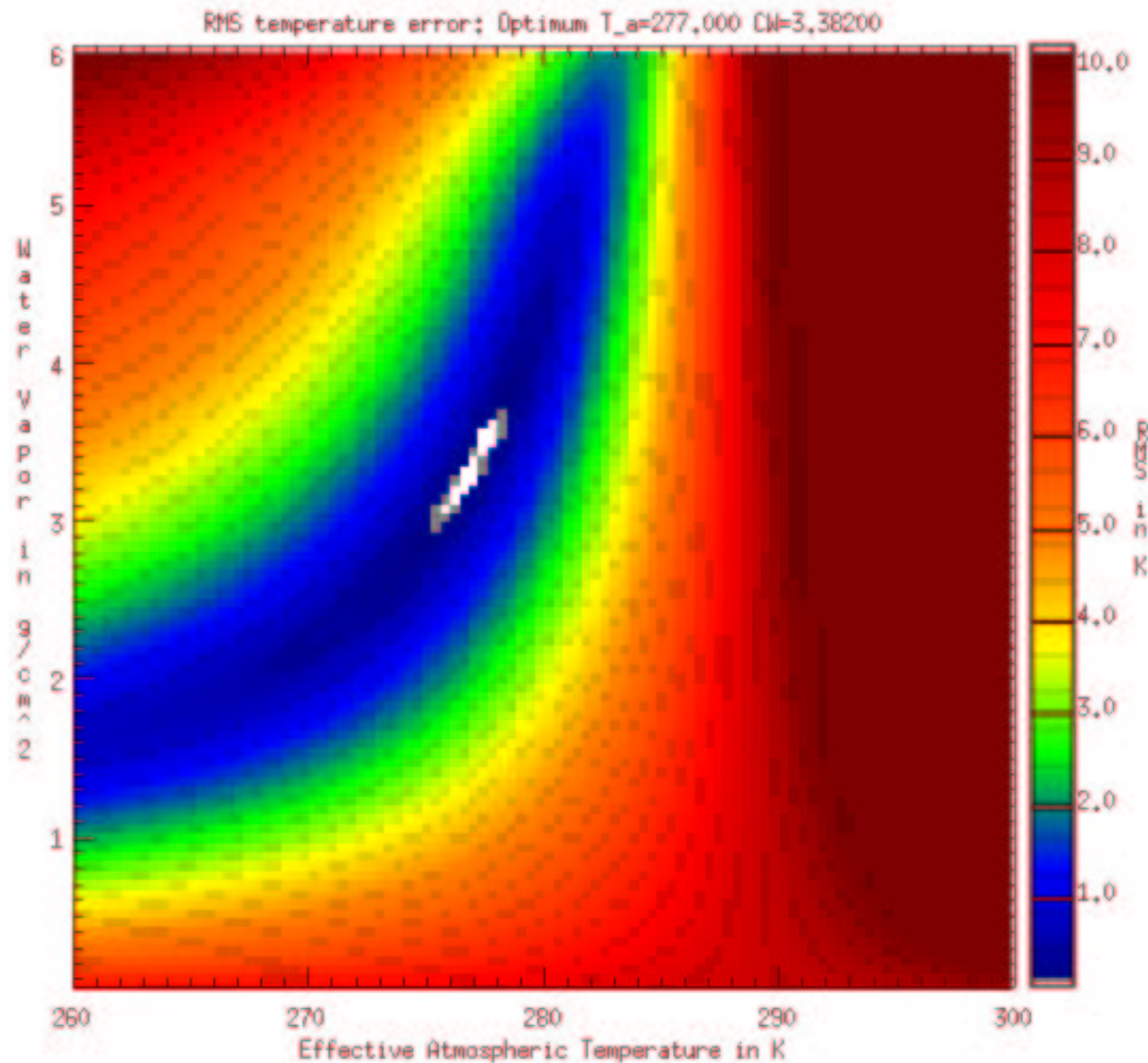
$$\hat{T}_w(i) = B_i^{-1} \left[ \frac{L_m(i) - B_i(T_a)[1 - \tau_i(CW)]}{(\varepsilon\tau)_i(CW)} \right],$$

over a range of  $CW$  and  $T_a$ , until the estimated water temperatures  $\hat{T}_{w,i}$  are most similar, i.e. minimize the standard deviation (STDEV) for a set of spectral channels  $i$  or mathematically:  $\sigma_k = STDEV(\hat{T}_{w,i}) = \text{minimum}$ .

- (b) Use the columnar water amount  $CW_{opt}$  and the effective atmospheric temperature  $T_{a,opt}$  which minimize  $STDEV(\hat{T}_{w,i})$  for the atmospheric correction of the radiance in all other water pixels.
3. Select the standard atmosphere  $k$  which is the best fit based on the smallest standard deviation  $\sigma_k$  of estimated water temperatures  $\hat{T}_{w,i}$ .

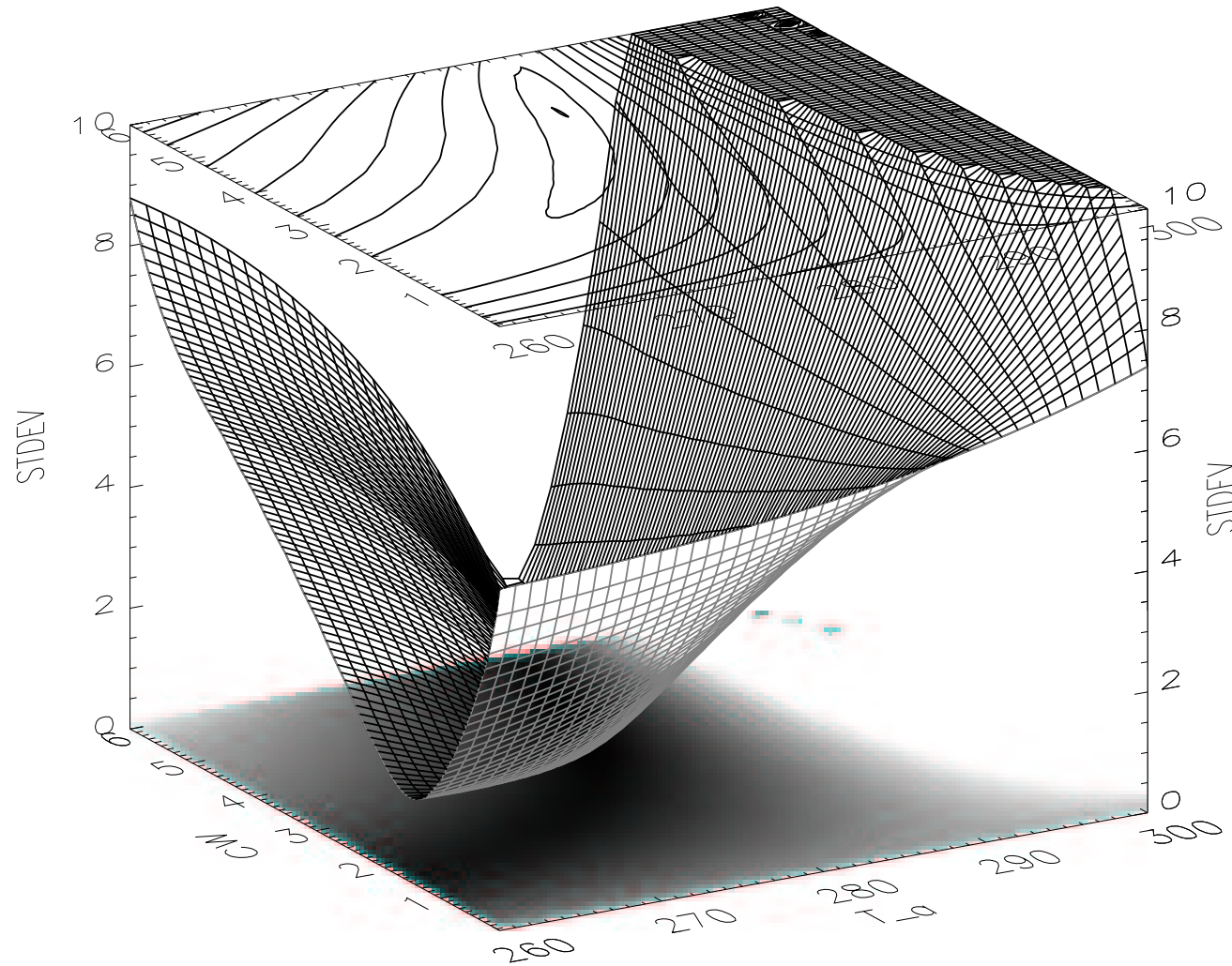


Standard deviation of the retrieved temperatures for channels KLMN as a function of effective atmospheric temperature  $T_a$  and columnar water vapor  $CW$ :



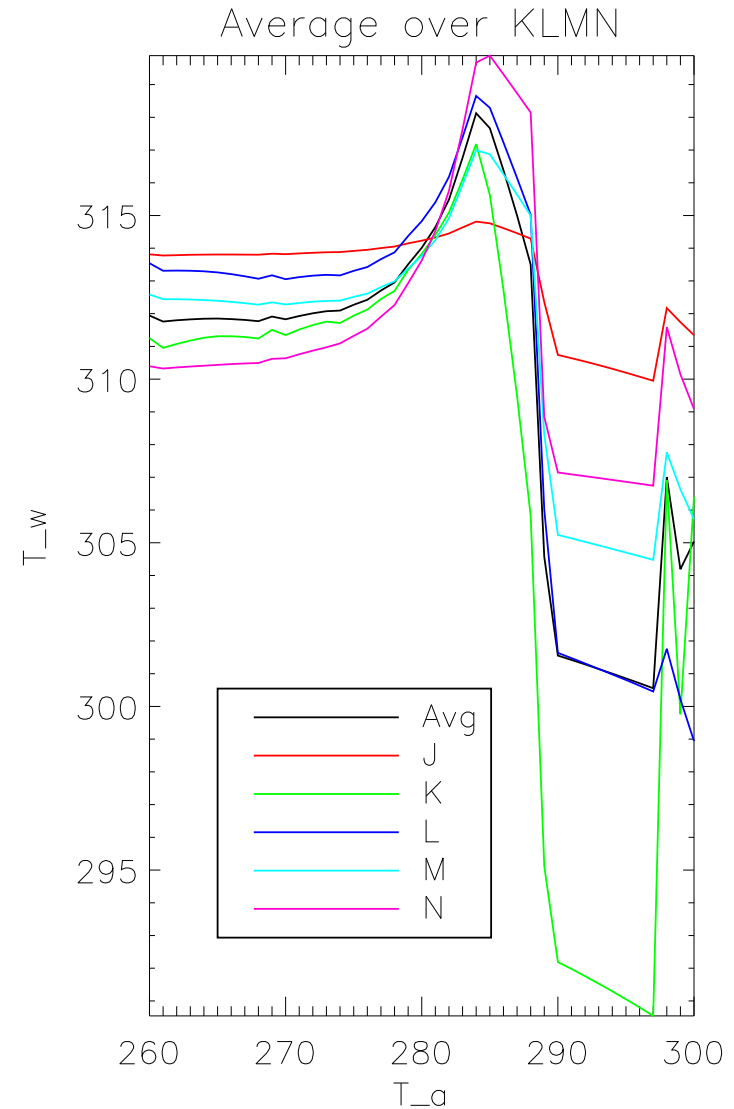
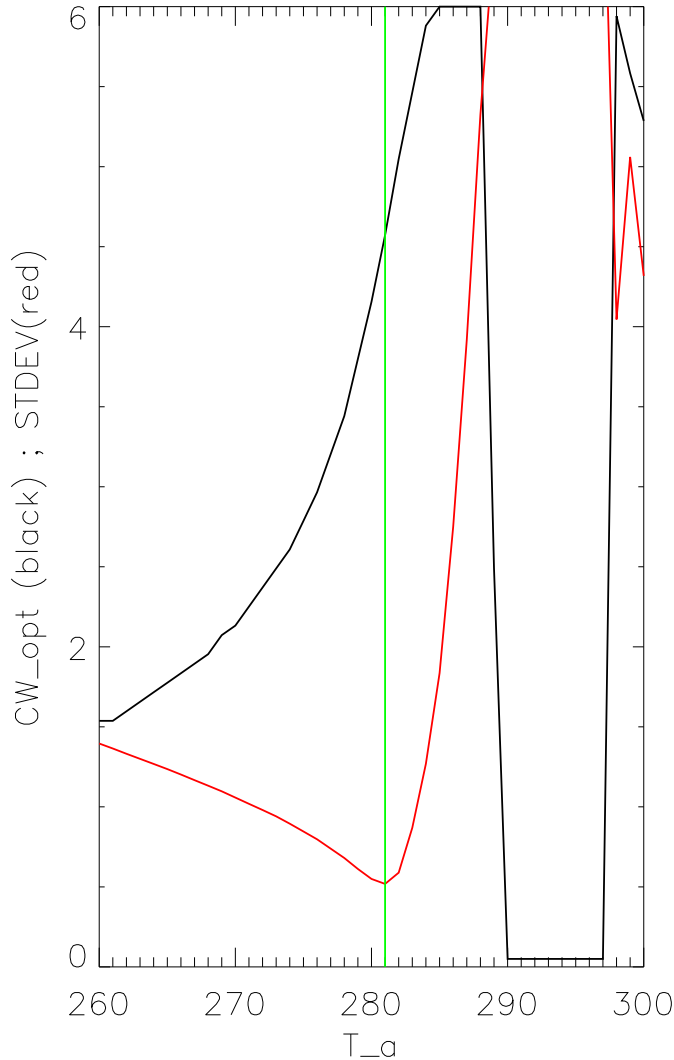
Note: White area is where  $STDEV(\hat{T}_{w,i})$  is minimum.

Standard deviation of the retrieved temperatures for channels KLMN as a function of effective atmospheric temperature  $T_a$  and columnar water vapor  $CW$ :



Standard deviation of the retrieved temperatures for channels KLMN as a function of effective atmospheric temperature  $T_a$  and columnar water vapor  $CW$ :

$T_a(\text{opt})=281.000$   $CW(\text{opt})=4.57200$



Minimum is where  $STDEV() = \min$  (left) and where  $T_w$  curves cross (right).

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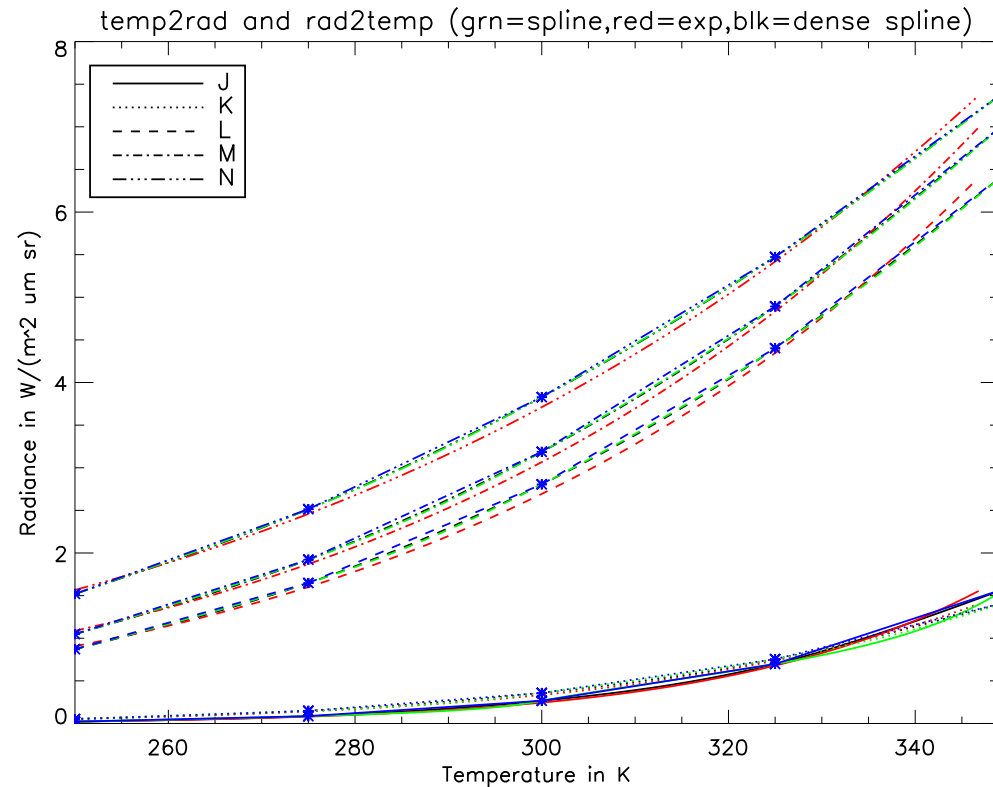
## *Convert from band averaged radiance to temperature and back*

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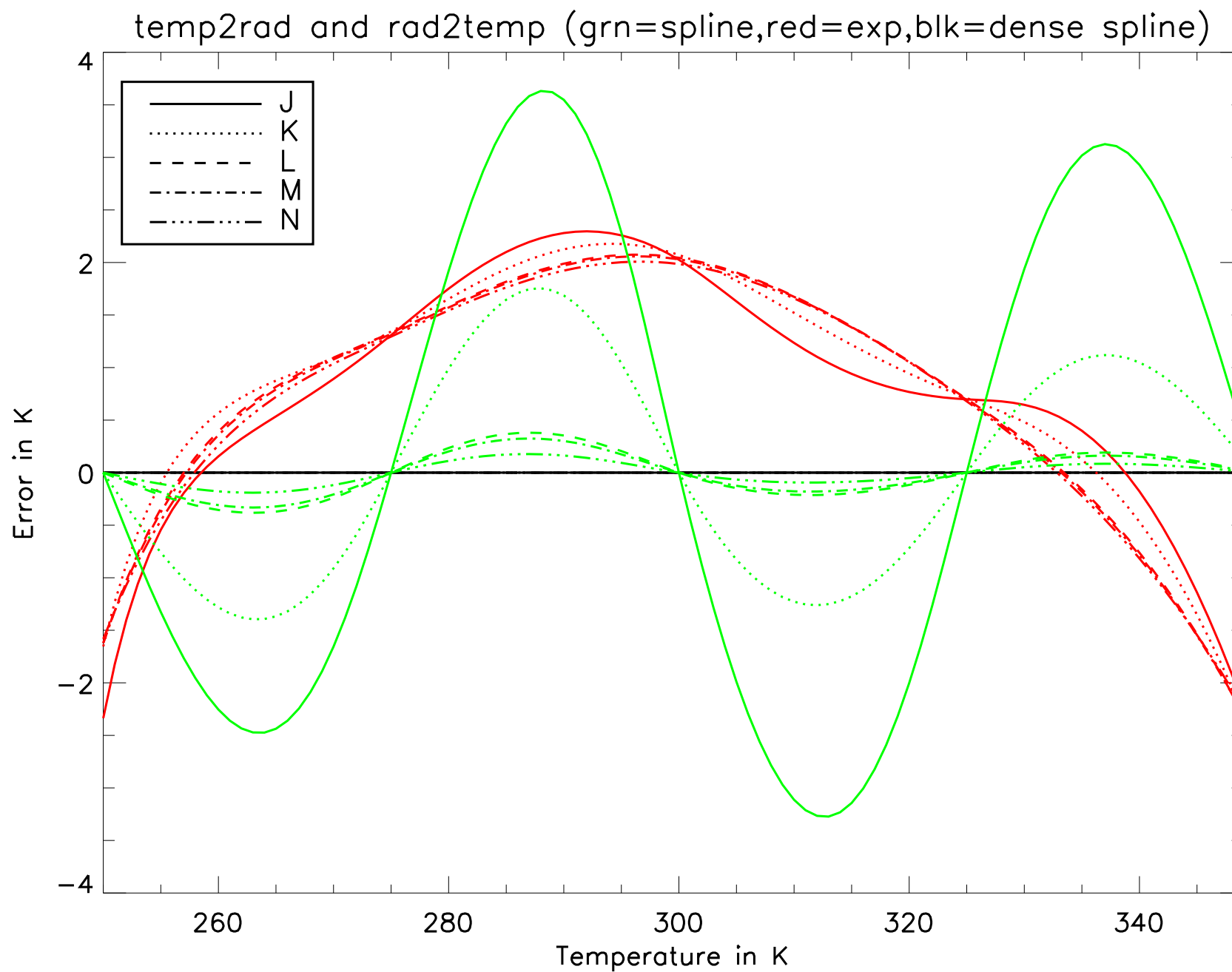
1. A quite natural way is to fit the temperature using  $T(L_i) = a_i(L_i)^{b_i}$ , where  $a_i=335.01, 335.13, 254.18, 246.34, 227.38$  and  $b_i=0.078379, 0.10109, 0.16729, 0.17586, 0.21137$ . Unfortunately this method creates systematic errors of up to 2 K compared to a spline interpolation which fits each calibration point exactly.
2. Converting from  $x$  =radiance to  $y$  =temperature can be done by spline interpolation using the 5 temperatures. We found however that the spline interpolation from temperature to radiance produced large oscillations of up to 3 K amplitude in channel J, 2 K in  $K$  and less than 0.4 K for  $L, M$  and  $N$ .
3. A better approach is to first increase the number of temperatures and radiances using  $x$  =radiance and  $y$  =temperature and second perform a spline interpolation with  $x$  =temperature and  $y$  =radiance. This will result in negligible temperature errors going from radiance to temperature and back.

# Band average radiance in $W/(m^2 \mu m sr)$ as a function of spectral channel and blackbody temperature

Blackbody temperature in K					
Channel	250.000	275.000	300.000	325.000	350.000
J ( $3.5\text{-}4.1 \mu m$ )	0.0396812	0.160335	0.499058	1.30691	2.98686
K ( $4.87\text{-}5.07 \mu m$ )	0.356723	1.02618	2.47562	5.21626	9.88215
L ( $8\text{-}8.4 \mu m$ )	2.88580	5.45944	9.29222	14.5840	21.4777
M ( $8.4\text{-}8.85 \mu m$ )	3.16871	5.80950	9.63493	14.7947	21.3864
N ( $10.2\text{-}10.7 \mu m$ )	3.88588	6.42711	9.78808	13.9924	19.0352



## Errors made by sparse and inaccurate fitting of table:





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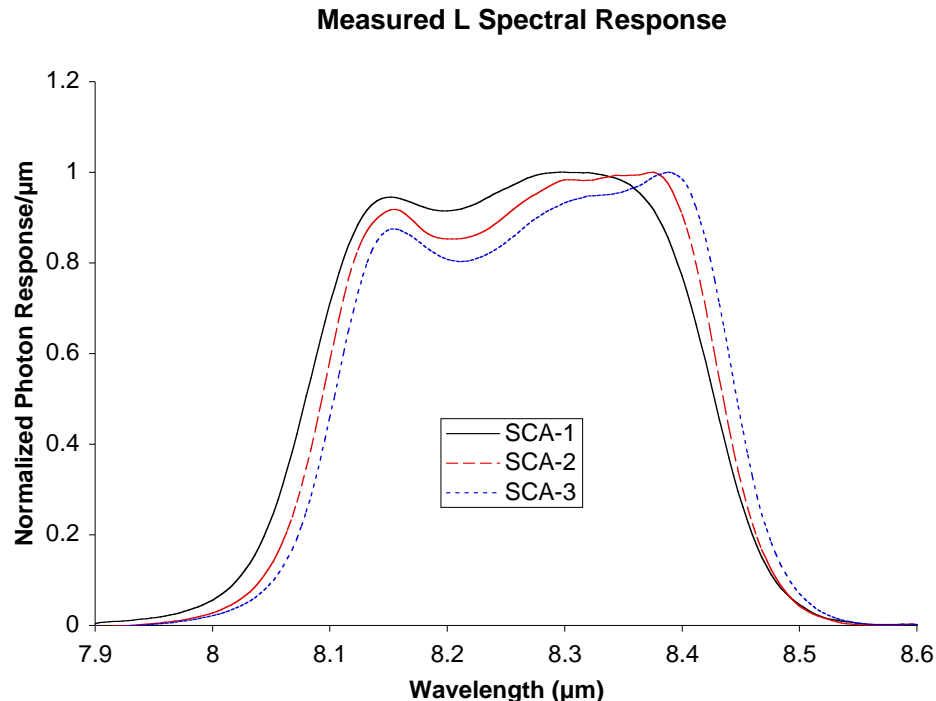
## *Effect of spectral shifts on atmospheric transmission*

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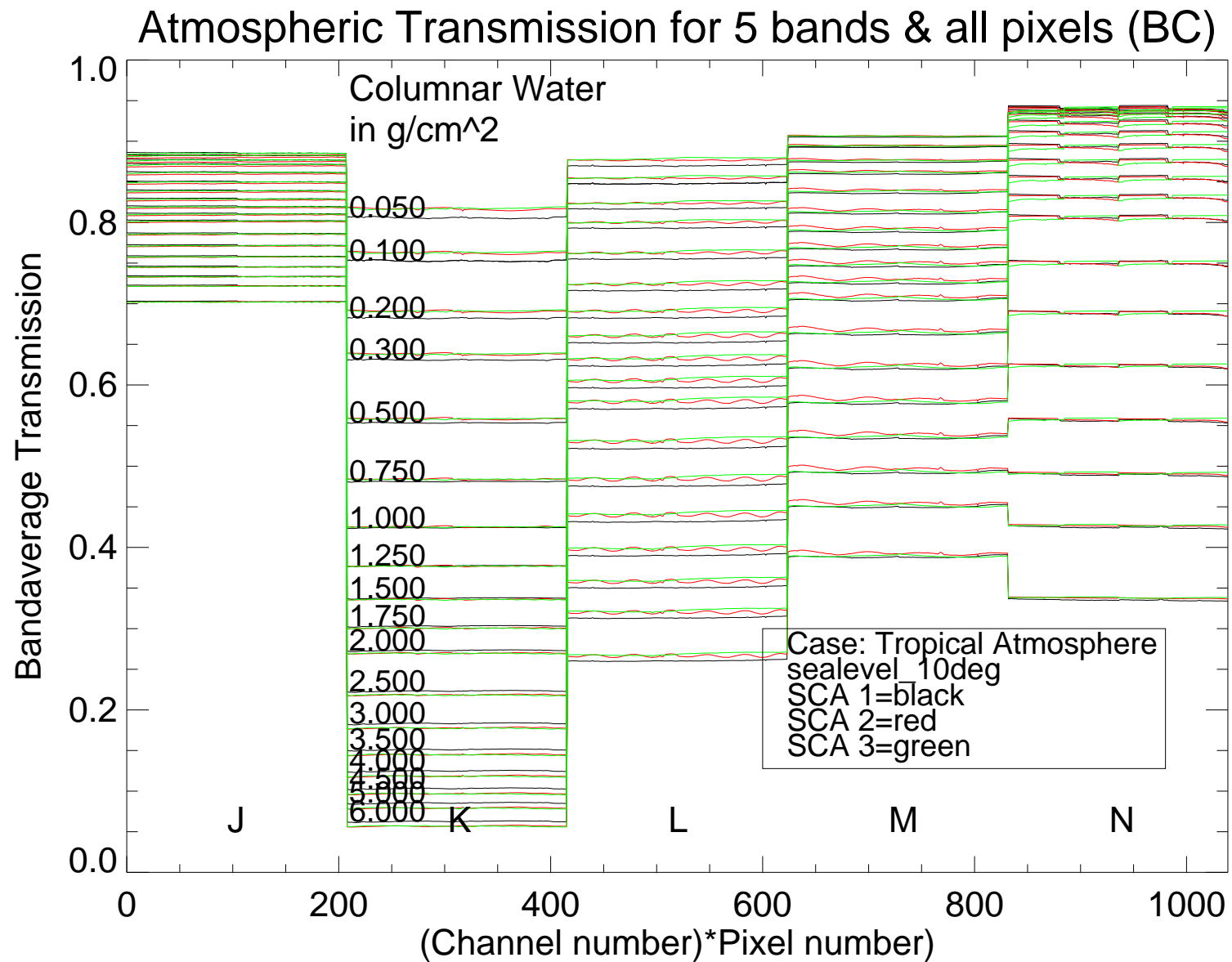
MTI's ground radiometric calibration based on:

- Filter functions measured at room temperature at nadir incidence
- Converted to pixel dependent filter functions at the actual incidence angles for a cone of light from a  $f3.5$  optical system at 75 K

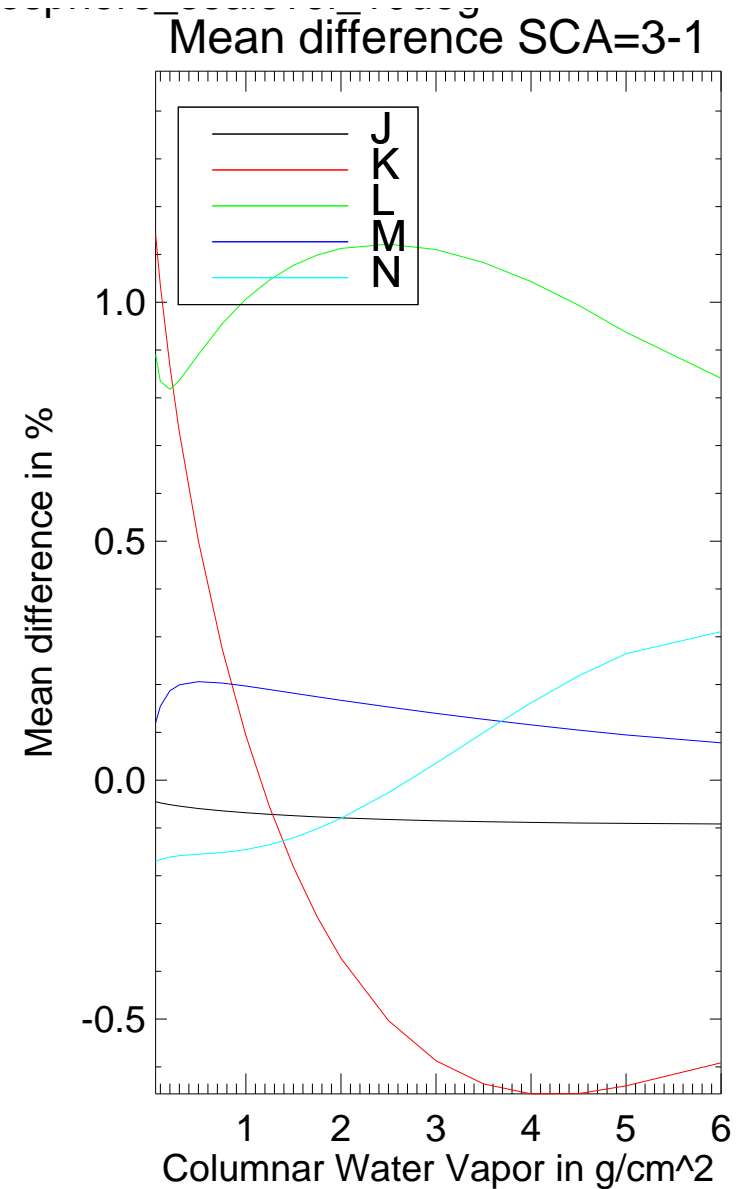
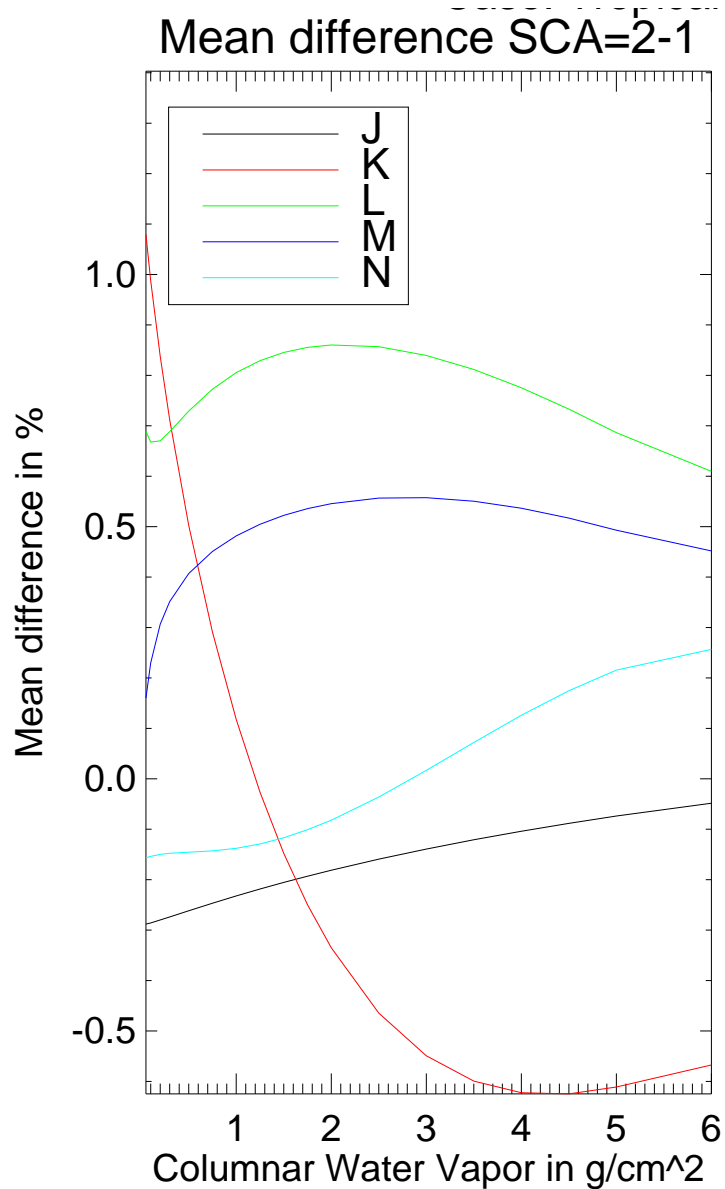
**Average spectral response for sub-chip assemblies 1, 2 and 3 for channel L:**



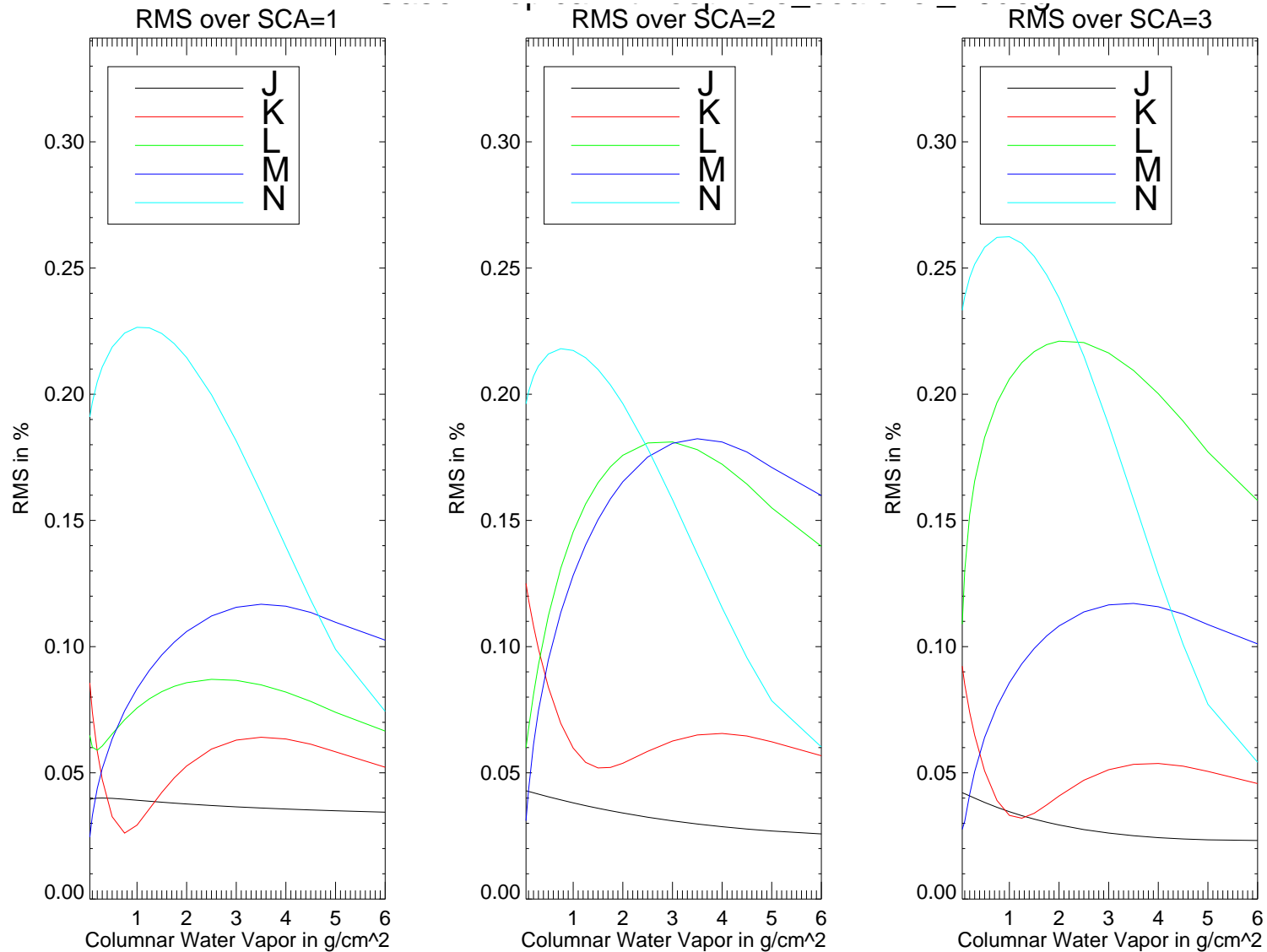
# Atmospheric transmission for each pixel as a function of water vapor:



## Atmospheric transmission difference between SCA's as a function of water vapor:



## RMS of transmission within a SCA as a function of water vapor:



Note: Interferences within SCA's cause a ripple of up to 0.25 %

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## *Recipe for a temperature/emissivity separation algorithm*

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### **Assumptions:**

1. The multi-spectral instrument has a channel  $j$  for which most emissivities reach a similar level, e.g. around  $11.5 \mu m$  many natural surfaces have emissivities between 0.95 and 0.97 (Salisbury and D'Aria, (1992)).
2. The atmosphere is homogeneous over the scene.

### **Algorithm:**

1. Determine the atmospheric parameters over water surfaces.
2. Apply the atmospheric correction to all pixel radiances:

$$L_{c,i} = \frac{L_{m,i} - B_i(T_{a,opt})[1 - \tau_i(CW_{opt})]}{(\varepsilon\tau)_i(CW)}.$$

3. Determine the skin temperature in the channel  $j$  assuming a fixed emissivity  $\varepsilon_{0,j}$ :

$$T_{s,j} = B_i^{-1}\left[\frac{L_{c,j}}{\varepsilon_{0,j}}\right].$$

4. Compute the emissivities in the other channels  $i \neq j$  by:

$$\varepsilon_i = \frac{L_{c,i}}{B_i(T_{s,j})}.$$

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## *Results*

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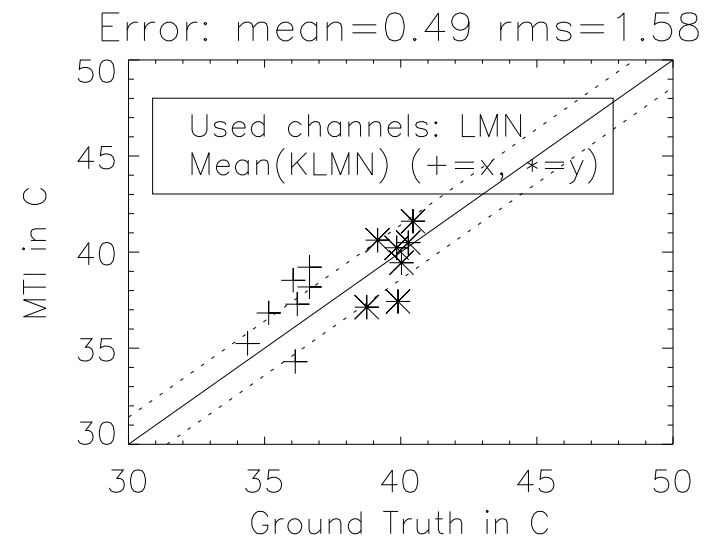
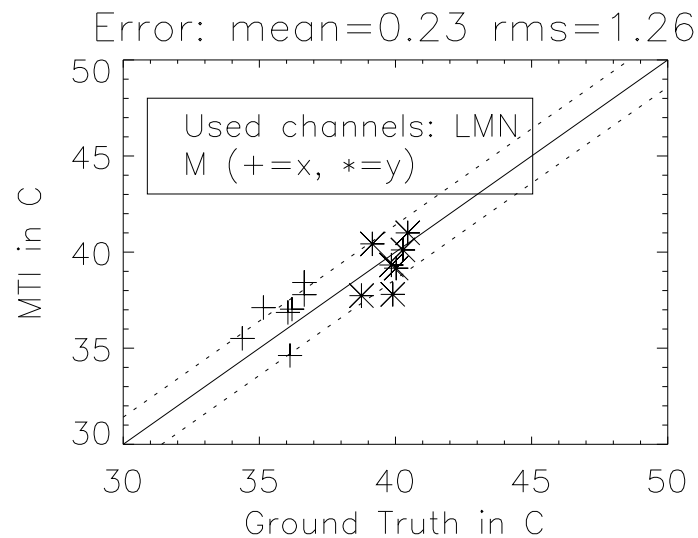
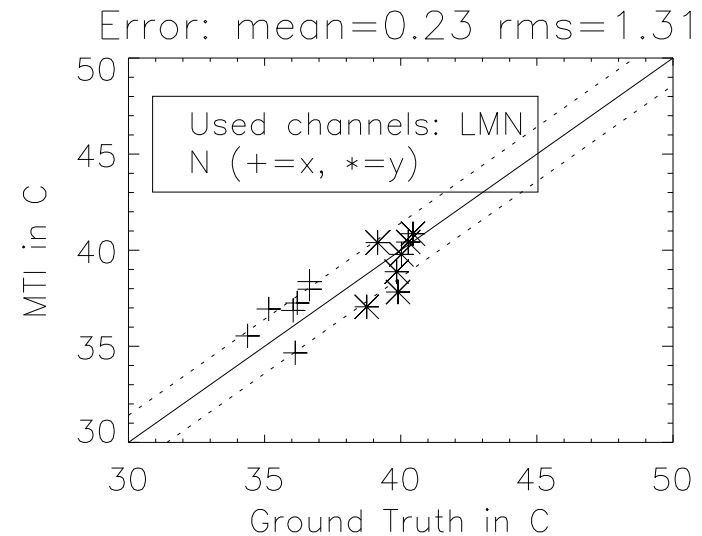
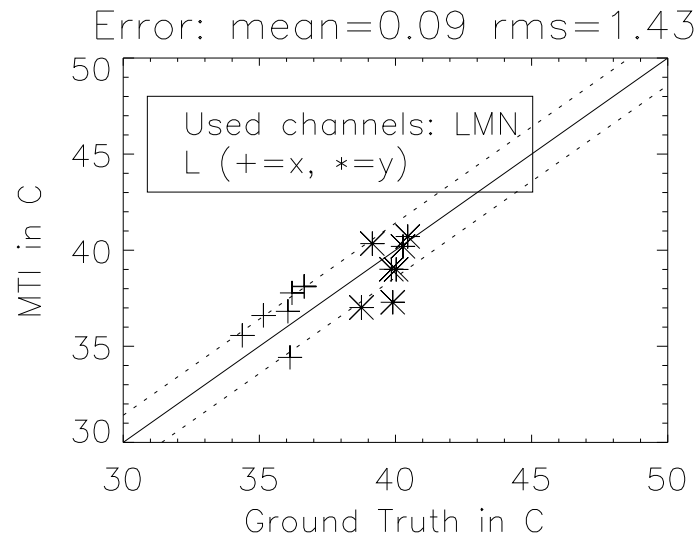
### **Sites:**

**Site A:** The Squaw Creek Reservoir in Texas is located in a hot and humid area where the bulk water temperatures range from  $34^{\circ}$  to  $40^{\circ}$  C during the observation period.

**Site B:** The Crater Lake in Oregon which is a very deep lake (600 m) at 1800 m altitude with temperatures ranging from  $5^{\circ}$  to  $17^{\circ}$  C over the observation period.

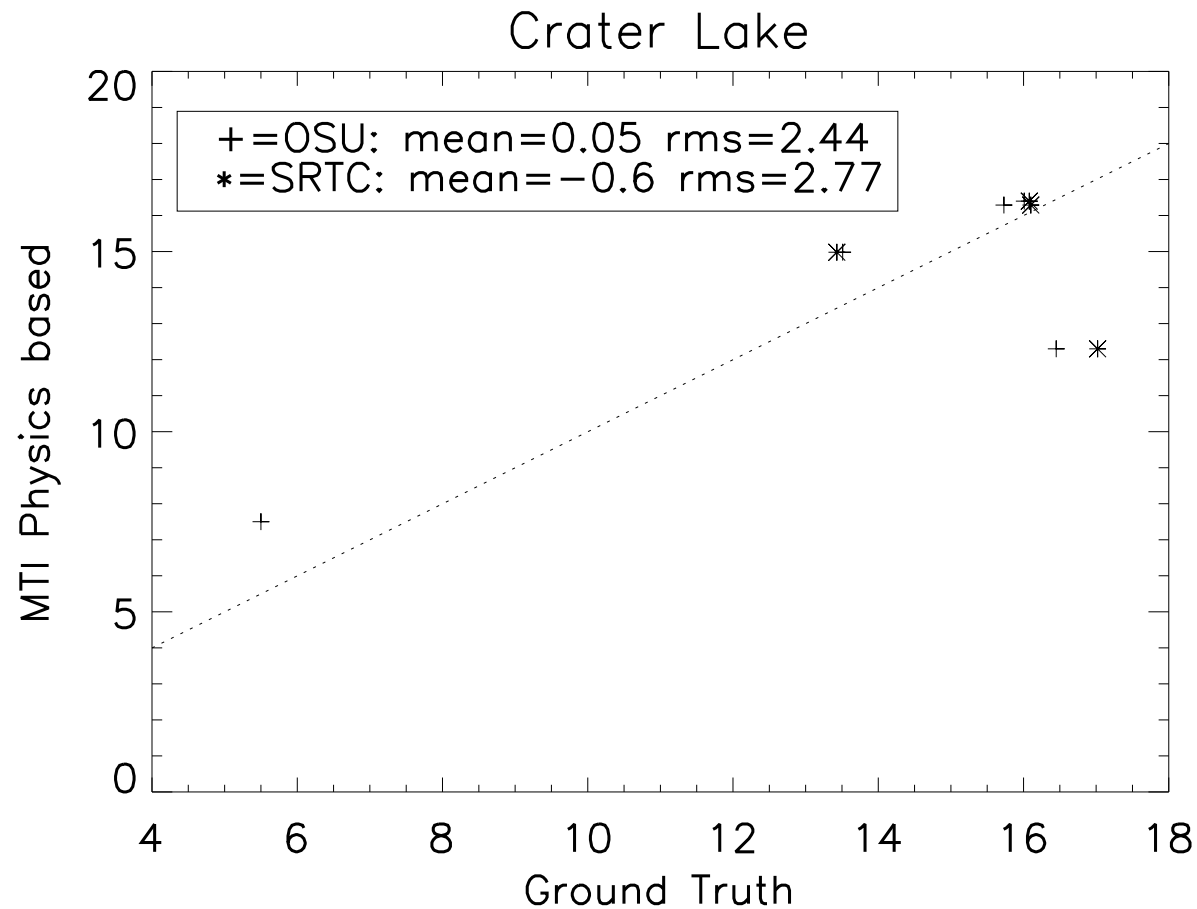
Both locations had precision sensors in place to measure the bulk water temperature.

Scatter plots with retrieved skin water temperature versus measured bulk water temperature for 2 sensor locations x and y and site A.



Best channel combination is LMN with rms=1.26 K

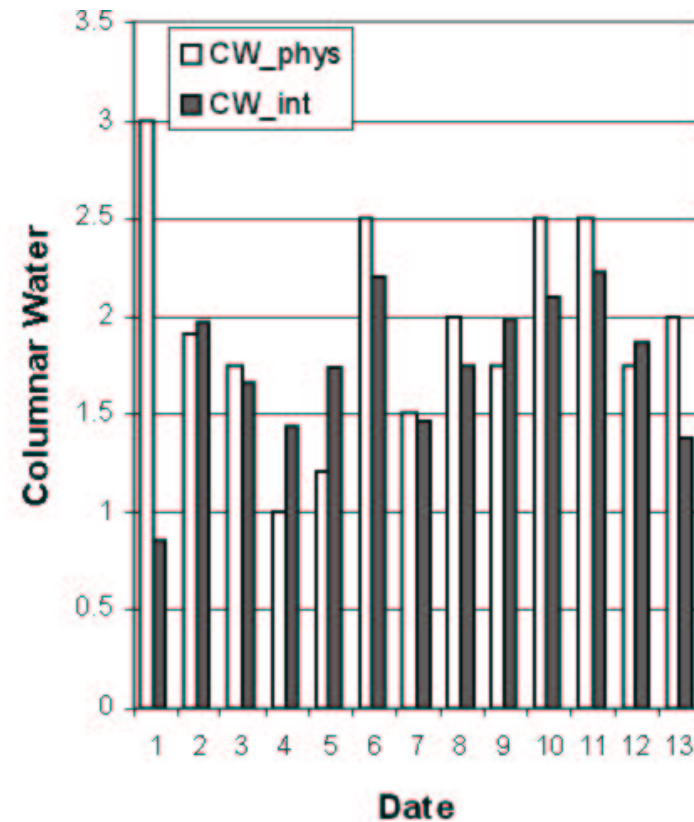
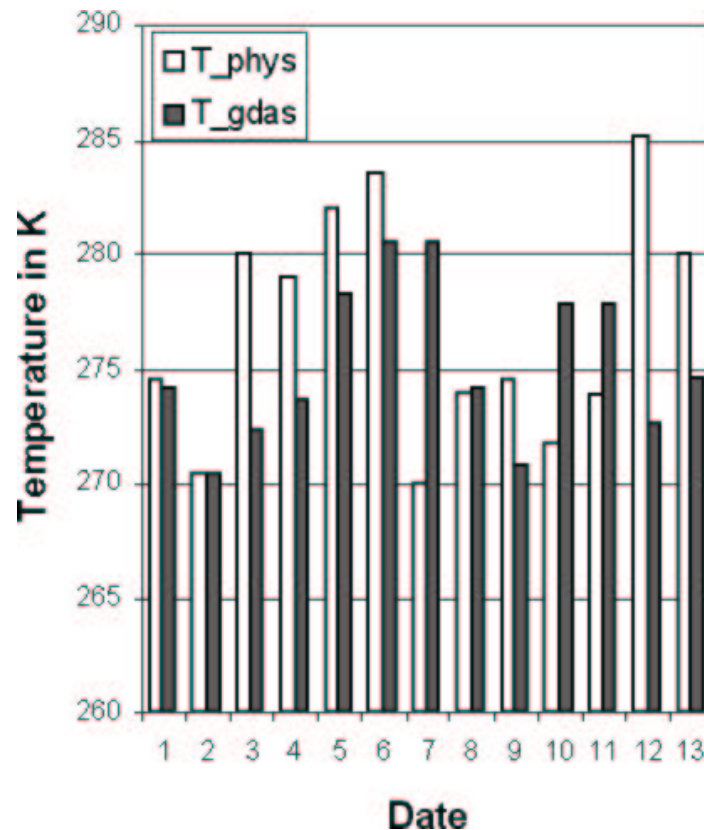
## Crater lake site:



- The mean difference to MTI retrievals was 0.05 K for OSU data and -0.66 K for SRTC data.
- The variance to MTI retrievals was 2.44 K for OSU and 2.72 K for SRTC.



## Comparison of retrieved atmospheric parameters with GDAS



- $RMSE(T_a(phys) - T_a(gdas))$  is 5.06 K
- $RMSE(PW(phys) - PW(gdas)) = 1.21$  for the water vapor

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## *Conclusions*

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- Method described in Borel et al, 1999 works for actual MTI data!
- Absolute temperature error is larger than predicted but probably due to small spectra filter shifts.
- Physics based retrievals of water temperatures is accurate to within  $\pm 1.5$  to 2 K.
- Retrieved atmospheric parameters seem reasonable compared with GDAS.

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## *Acknowledgements*

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